	SSG: INVERTERS THAT MIMIC SYNCHRONOUS GENERATORS		
	Qing-Chang Zhong	George Weiss	
UNIVERSITY OF LIVERPOOL	Electrical Drives, Power and Control Group	Department of Electrical Engineering Systems	
	Department of Electrical Engineering & Electronics	Faculty of Engineering	
	The University of Liverpool, UK	Tel Aviv University, Israel	
	Email: Q.Zhong@liv.ac.uk	E-mail: gweiss@eng.tau.ac.il	

# Abstract

In this poster, the idea of operating an inverter to mimic a synchronous generator is developed. We call the inverters that are operated in this way static synchronous generators (SSG). This means that the well-established theory/algorithms used to control synchronous generators can still be used in power systems where a significant proportion of the generating capacity is inverter-based. The implementation and operation of SSGs are described in detail. The real and reactive power delivered by SSGs connected in parallel can be automatically shared using the well-known frequency and voltage drooping mechanism. SSGs can also be easily operated in island mode and hence they provide an ideal solution for micro-grids or smart grids. Both simulation and experimental results are given to verify the idea.

where J is the moment of inertia of all parts rotating with the rotor,  $T_m$  is the mechanical torque,  $T_e$ is the electromagnetic toque and  $D_p$  is a damping factor.  $T_e$  can be found from the energy E stored in the machine magnetic field, *i.e.*,

 $E = \frac{1}{2} \langle i, \Phi \rangle + \frac{1}{2} i_f \Phi_f$ =  $\frac{1}{2} \langle i, L_s i \rangle + M_f i_f \langle i, \widetilde{\cos} \theta \rangle + \frac{1}{2} L_f i_f^2.$ 

From simple energy considerations, we have

 $T_e = \frac{\partial E}{\partial \theta_m} \bigg|_{\Phi, \Phi_f \text{ constant}} = -\frac{\partial E}{\partial \theta_m} \bigg|_{i, i_f \text{ constant}}$ Since the mechanical rotor angle  $\theta_m$  satisfies  $\theta =$  $p\theta_m,$ (7) These coincide with the conventional definitions for real power and reactive power. The equation (6) can be written as

$$\ddot{\theta} = \frac{1}{J}(T_m - T_e - D_p \dot{\theta}),$$

where the input is the mechanical torque  $T_m$ , while the electromagnetic torque  $T_e$  depends on i and  $\theta$ , according to (7). This equation, together with (7), (8) and (9), are implemented in the electronic part of an SSG.

## 3. Operation of an SSG

### Frequency drooping and regulation of real power



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1. Modeling of synchronous generators

Electrical part

We consider a round rotor machine (without damper windings), with p pairs of poles per phase (and p pairs of poles on the rotor) and with no saturation effects in the iron core. The stator windings can be regarded as concentrated coils having self-inductance L and mutual inductance -M, as shown in the figure below.



The field (or rotor) winding can be regarded as a concentrated coil having self-inductance  $L_f$ . The mutual inductance between the field coil and each of the three stator coils varies with the (electrical) rotor angle  $\theta$  as follows:

> $M_{af} = M_f \cos(\theta),$  $M_{hf} = M_f \cos(\theta - \theta)$

 $T_e = p M_f i_f \left\langle i, \, \widetilde{\sin \theta} \right\rangle.$ 

Note that if  $i = i_0 \sin \varphi$  (as would be the case in sinusoidal steady state), then

 $T_e = pM_f i_f i_0 \left\langle \widetilde{\sin \varphi}, \, \widetilde{\sin \theta} \right\rangle = \frac{3}{2} pM_f i_f i_0 \cos(\theta - \varphi).$ 

Note also that if  $i_f$  is constant (as is usually the case), then (7) with (4) yields

 $T_e \dot{\theta}_m = \langle i, e \rangle$ .

2. Implementation of a static synchronous generator

A simple DC/AC converter (inverter) used to convert DC power into three-phase AC is what we call the power part of the SSG. What we call the electronic part is a program running in a processor, which controls the switches in the power part. These two parts interact via the signals e and i (vand  $v_q$  will be used for controlling the SSG).

# The power part

This part consists of three phase legs and a threephase LC filter, which is used to suppress the switching noise. If the inverter is to be connected to the grid, then three more inductors inductors  $L_q$ (with series resistance  $R_q$ ) and a circuit breaker are needed to interface with the grid.

The speed regulation system of the prime mover for a conventional synchronous generator can be implemented in an SSG by comparing the virtual angular speed  $\theta$  with the angular frequency reference  $\theta_r$ , e.g. the nominal angular speed  $\theta_n$ , before feeding it into the damping block  $D_p$ . As a result, the damping factor  $D_p$  actually behaves as the frequency drooping coefficient, which is defined as the ratio of the required change of torque  $\Delta T$  to the change of speed (frequency)  $\Delta \theta$ . That is,

 $D_p = \frac{\Delta T}{\Delta \dot{\theta}} = \frac{\Delta T}{T_{mn}} \frac{\dot{\theta}_n}{\Delta \dot{\theta}} \frac{T_{mn}}{\dot{\theta}_n},$ 

where  $T_{mn}$  is the nominal mechanical torque. Because of the built-in frequency drooping mechanism, an SSG automatically shares the load with other inverters of the same type and with SGs connected on the same bus.



Regulation of real and reactive power The regulation mechanism of the real power (torque) has a cascaded control structure, of which the inner loop is the frequency (speed) loop and the

) 0.5 1 1.5 2 2.5 3 3.5 4 4.5 5 5.5 6 Time (Second) 5. Experimental results



$$M_{cf} = M_f \cos(\theta - \frac{3}{4\pi}).$$
Define
$$\Phi = \begin{bmatrix} \Phi_a \\ \Phi_b \\ \Phi_c \end{bmatrix}, \quad i = \begin{bmatrix} i_a \\ i_b \\ i_c \end{bmatrix}$$
and

$$\widetilde{\cos \theta} = \begin{bmatrix} \cos \theta \\ \cos(\theta - \frac{2\pi}{3}) \\ \cos(\theta - \frac{4\pi}{3}) \end{bmatrix}, \quad \widetilde{\sin \theta} = \begin{bmatrix} \sin \theta \\ \sin(\theta - \frac{2\pi}{3}) \\ \sin(\theta - \frac{4\pi}{3}) \end{bmatrix}$$

Assume that the neutral line is not connected, then

 $i_a + i_b + i_c = 0.$ 

The stator flux linkages are

and

$$\Phi = L_s i + M_f i_f \widetilde{\cos} \theta, \qquad (1)$$

(2)

(5)

where  $L_s = L + M$ , and the field flux linkage is

 $\Phi_f = L_f i_f + M_f \left\langle i, \, \widetilde{\cos} \theta \right\rangle,$ 

where  $\langle \cdot, \cdot \rangle$  denotes the conventional inner product. The second term  $M_f \langle i, \widetilde{\cos \theta} \rangle$  is constant if the three phase currents are sinusoidal (as functions of  $\theta$ ) and balanced. Assume that the resistance of the stator windings is  $R_s$ , then the phase terminal voltages  $v = \begin{bmatrix} v_a & v_b & v_c \end{bmatrix}^T$  can be obtained from (1) as



The power part of a static synchronous generator (SSG) is a basic inverter

It is advantageous to assume that the field (rotor) winding of the SSG is fed by an adjustable DC current source  $i_f$  instead of a voltage source  $v_f$ . In this case, the terminal voltage  $v_f$  varies, but this is irrelevant. As long as  $i_f$  is constant, the generated voltage from (4) is

> $e = \dot{\theta} M_f i_f \widetilde{\sin \theta}.$ (8)

The switches in the inverter are operated so that the average values of  $e_a$ ,  $e_b$  and  $e_c$  over a switching period should be equal to e given in (8), which can be achieved by the usual PWM technique.



The electronic part of an SSG (without control)

The electronic part

outer loop is the real power (torque) loop. The time constant of the frequency loop is  $\tau_f = \frac{J}{D_n}$ . In other words, J can be chosen as

$$J = D_p \tau_f.$$

# Voltage drooping and regulation of reactive power

The regulation of reactive power Q flowing out of the SSG can be realized similarly. Define the voltage drooping coefficient  $D_q$  as the ratio of the required change of reactive power  $\Delta Q$  to the change of voltage  $\Delta v$ , *i.e.*,

$$D_q = \frac{\Delta Q}{\Delta v} = \frac{\Delta Q}{Q_n} \frac{v_n}{\Delta v} \frac{Q_n}{v_n},$$

where  $Q_n$  is the nominal reactive power and  $v_n$  is the nominal amplitude of terminal voltage v. The difference between the reference voltage  $v_r$  and the amplitude of the feedback voltage  $v_{fb}$  is amplified with the voltage drooping coefficient  $D_q$  before adding to the difference between the set point  $Q_{set}$ and the reactive power Q. The resulting signal is then fed into an integrator with a gain  $\frac{1}{K}$  to generate  $M_f i_f$ . Similarly, K can be chosen as

# $K = \dot{\theta}_n D_q \tau_v,$

where  $\tau_v$  is the time constant of the voltage loop.

7) stop data recording, roughly at 27s. During this experiment, the grid frequency was higher than 50Hz, increasing from 50.11Hz to 50.15Hz.



$$v = -R_s i - \frac{\mathrm{d}\Phi}{\mathrm{d}t} = -R_s i - L_s \frac{\mathrm{d}i}{\mathrm{d}t} + e, \quad (3)$$

where  $e = \begin{bmatrix} e_a & e_b & e_c \end{bmatrix}^T$  is the back emf due to the rotor movement given by

> $e = M_f i_f \dot{\theta} \widetilde{\sin \theta} - M_f \frac{\mathrm{d}i_f}{\mathrm{d}t} \widetilde{\cos \theta}.$ (4)

The field terminal voltage, from (2), is

 $v_f = -R_f i_f - \frac{\mathrm{d}\Phi_f}{\mathrm{d}t},$ 

where  $R_f$  is the resistance of the rotor winding. However, we shall not need the expression for  $v_f$ because we shall use  $i_f$ , instead of  $v_f$ , as an adjustable constant input.

Mechanical part

The mechanical part of the machine is governed by (6)

 $J\ddot{\theta} = T_m - T_e - D_p \dot{\theta},$ 

Define the generated real power P and reactive power Q (as seen from the inverter legs) as

 $P = \langle i, e \rangle$  and  $Q = \langle i, e_q \rangle$ ,

where  $e_q$  has the same amplitude as e but with a phase delayed from that of e by  $\frac{\pi}{2}$ , *i.e.*,

 $e_q = \dot{\theta} M_f i_f \widetilde{\sin}(\theta - \frac{\pi}{2}) = -\dot{\theta} M_f i_f \widetilde{\cos} \theta.$ 

Then, the real power and reactive power are

 $P = \dot{\theta} M_f i_f \left\langle i, \, \widetilde{\sin} \, \theta \right\rangle,$ 

 $Q = -\dot{\theta} M_f i_f \left\langle i, \, \widetilde{\cos} \, \theta \right\rangle.$ (9)Note that if  $i = i_0 \sin \varphi$ , then

 $P = \dot{\theta} M_f i_f \left\langle i, \, \widetilde{\sin \theta} \right\rangle = \frac{3}{2} \dot{\theta} M_f i_f i_0 \cos(\theta - \varphi),$  $Q = -\dot{\theta}M_f i_f \langle i, \, \widetilde{\cos}\theta \rangle = \frac{3}{2}\dot{\theta}M_f i_f i_0 \sin(\theta - \varphi).$ 

4. Simulation results

The parameters of the inverter for carrying out the simulations are given in the Table below.

Parameters	Values	Parameters	Values
$L_s$	0.45 mH	$L_g$	0.45 mH
$R_s$	$0.135\Omega$	$R_g$	$0.135\Omega$
C	$22\mu\mathrm{F}$	Frequency	50 Hz
R	$1000\Omega$	Line voltage	20.78 Vrms
Rated power	100 W	DC voltage	42V
$D_p$	0.2026	$D_q$	117.88

The simulation was started at t = 0 to allow the PLL and SSG to start-up (in real applications, these two can be started separately). The dynamics in the first half second will be omitted. The circuit breaker was turned on at t = 1s; the real power  $P_{set} = 80W$  was applied at t = 2s and the reactive power  $Q_{set} = 60$ Var was applied at t = 3s. The drooping mechanism was enabled at t = 4s and then the grid voltage decreased by 5% at t = 5s.

### 6. Potential applications

• Distributed generation and renewable energy, such as combined heat and power (CHP), wind and solar power. The SSG technology allows these sources to take part in the regulation of power system frequency, voltage and overall stability.

• Uninterrupted power supplies (UPS), in particular, the parallel operation of multiple UPSs

• Isolated/distributed power supplies, e.g. to replace rotary frequency converters

• Induction heating

• Static synchronous compensator (STATCOM) to improve power factor

• HVDC transmission (at the receiving end)