We demonstrate an all-optical phase noise mitigation scheme based on the generation, delay, and coherent summation of higher order signal harmonics. The signal, its third-order harmonic, and their corresponding delayed variant conjugates create a staircase phase-transfer function that quantizes the phase of quadrature-phase-shift-keying (QPSK) signal to mitigate phase noise. The signal and the harmonics are automatically phase-locked multiplexed, avoiding the need for phase-based feedback loop and injection locking to maintain coherency. The residual phase noise converts to amplitude noise in the quantizer stage, which is suppressed by parametric amplification in the saturation regime. Phase noise reduction of \( \sim 40\% \) and OSNR-gain of \( \sim 3 \) dB at BER \( 10^{-3} \) are experimentally demonstrated for 20- and 30-Gbaud QPSK input signals.

Advanced modulation formats such as quadrature-phase-shift-keying (QPSK) are gaining importance in high capacity optical networks \([1,2]\). In QPSK systems, phase or amplitude noise can cause a degradation in the received data’s signal-to-noise ratio, resulting in a system power penalty. In specific, phase noise originating from interaction of ASE noise and Kerr nonlinearity can pose a key limitation in such systems \([3,4]\).

Nonlinear phase noise of a high data rate signal can be reduced by taking advantage of electronic-based parallel data-processing techniques \([2,5,6]\). However, there might be advantages to mitigate the phase noise in the optical domain, such as avoiding the impact of optical-to-electronic conversion and supporting in-line signal processing for high-baud-rate signal \([6]\). Different approaches have been demonstrated for optical regeneration of QPSK signals using different variations of phase-sensitive amplification to achieve a level of “phase squeezing” \([7–9]\). However, these methods tend to require coherency between a signal and a pump, typically requiring phase-based feedback loops and injection locking lasers \([7–10]\).

Here, we propose and experimentally demonstrate a baud-rate-tunable phase-noise-mitigation scheme. Phase noise is mitigated in an all-optical phase quantizer by combining the signal, the conjugate copy, and their delayed variant third harmonics. In the proposed method, the signal and the harmonics are automatically phase-locked multiplexed, avoiding the need for phase-based feedback loop and injection locking to maintain coherency. The residual phase noise converts to amplitude noise \([7,11]\). Such converted amplitude noise can be compensated by means of an amplitude limiter.

The conceptual block diagram of the proposed approach is shown in Fig. 1. A QPSK signal contaminated with phase noise is coupled with a CW pump, and injected into a nonlinear wave mixer to generate a phase conjugate copy of the signal \([12]\). The signal and the conjugate copy are then sent into a medium to generate the third-order harmonics of the signal and the conjugate copy. In fact, these two stages can be combined in one stage by using a element with high amount of nonlinear efficiency \([13]\). The signal, its third-order harmonic,
and their conjugates are sent into an optical programmable filter to apply appropriate delays and adjust amplitudes and relative phases. The adjusted signals and harmonics with a CW pump are injected into a nonlinear medium to create a staircase phase-transfer function. In this stage, the product of the signal and its delayed conjugate, and the product of the delayed third-order signal harmonic and the conjugate third-order harmonic are phase-locked multiplexed. This nonlinear process builds a staircase phase-transfer function of the input signal, which results in squeezing the phase noise of the input signal. The residual phase noise that is not squeezed in the phase quantization process converts to amplitude noise due to the nonuniform amplitude profile of the staircase phase-transfer function. The amplitude noise is suppressed by utilizing an optical parametric amplifier operated in the saturation regime.

In the following, the mathematical descriptions of nonlinear stages to create the phase quantization function are presented.

A periodically poled lithium niobate (PPLN) waveguide is used in the first nonlinear stage. The pump \( P_1(t) \) interacts with itself through a second-harmonic-generation process, and creates the mixing term \( P_1^2(t) \) at 2\( \omega_{p1} \). The SHG term then mixes with the input signal \( S_{in}(t) \) through the difference-frequency-generation (DFG) process to create a phase conjugate replica with the electric field proportional to \( P_1^2(t) \times S_{in}^* (t) \). The PPLN-1 output is sent into an in-line spatial light modulator (SLM) to filter out the pump. The signal and its conjugate are mixed through a four-wave-mixing process in a highly nonlinear fiber (HNLF) to generate the third-order harmonics. The electric field of the generated third-order harmonics is proportional to 

\[
E_{3}(t) \propto P_1^2(t - T_s) \times S_{in}^* (t - T_s) \times S_{in}^3(t).
\]

Similarly, the generated third-order harmonics are mixed through an SFG process and generate a new signal \( E_3(t) \) at 2\( \omega_{p1} \):

\[
E_3(t) \propto P_1^2(t - T_s) \times P_1^3(t) \times S_{in}^* (t - T_s) \times S_{in}^3(t) \times S_{in}^3(t).
\]

The challenge of combining the signals \( E_1(t) \) and \( E_2(t) \) at 2\( \omega_{p1} \) result from the fact that they need to be phase locked and have the same phase reference. According to Eqs. (1) and (2), the phases of \( E_1(t) \) and \( E_2(t) \) can be expressed as

\[
\Phi_{E1}(t) = 2\Phi_{p1}(t - T_s) + \Delta\Phi_{in}(t),
\]

\[
\Phi_{E2}(t) = -2\Phi_{p1}(t - T_s) + 4\Phi_{p1}(t) - 3\Delta\Phi_{in}(t)
\]

\[
= 2\Phi_{p1}(t - T_s) + 4\Delta\Phi_{p1}(t) - 3\Delta\Phi_{in}(t),
\]

where \( \Phi_{in}(t) \) and \( \Phi_{p1}(t) \) refer to the phase of the input signal and the pump, respectively. Moreover, \( \Delta \) is defined as a difference operator for one symbol interval \( T_s \), i.e.,

\[
\Delta\Phi(t) \triangleq \Phi(t) - \Phi(t - T_s).
\]

In order to study the coherence of \( E_1(t) \) and \( E_2(t) \), the phase noise of the input signal, \( \Phi_{in}^N(t) \), and the phase noise of the pump, \( \Phi_{p1}^N(t) \), need to be considered in Eqs. (3) and (4), except for the first similar term \( 2\Phi_{p1}(t - T_s) \):

\[
\Phi_{E1}(t) = 2\Phi_{p1}(t - T_s) + \Delta\Phi_{in}^D(t) + \Delta\Phi_{in}^N(t),
\]

\[
\Phi_{E2}(t) = 2\Phi_{p1}(t - T_s) + 4\Delta\Phi_{in}^N(t) + \Delta\Phi_{in}^D(t) - 3\Delta\Phi_{in}^N(t),
\]

where \( \Phi_{in}^D(t) \) refers to the QPSK data, and \( \Delta\Phi_{in}^D(t) \) represents the simple encoded version of the original signal. Equation (5) uses the fact that for QPSK data \( \exp(-j\Delta\Phi_{in}^D(t)) = \exp(j\Phi_{in}(t)) \); and the term \( -3\Delta\Phi_{in}^D(t) \) is replaced by \( \Delta\Phi_{in}^D(t) \).

Assuming that the phase noise of the pump, \( \Phi_{p1}^N(t) \), is from the laser linewidth (\( \Delta\nu \)), and its fluctuation is significantly slower than the symbol rate (\( \Delta\nu \ll 1/T_s \)), we conclude that

\[
\Delta\Phi_{p1}^N(t) = \Phi_{p1}^N(t) - \Phi_{p1}^N(t - T_s) \text{ is negligible.}
\]

By performing Fourier transform of \( \Delta\Phi_{p1}^N(t) \), the result is

\[
\mathcal{F}(\Delta\Phi_{p1}^N(t)) \triangleq 2\exp\left(-\frac{j\omega T_s}{2}\right) \sin\left(\frac{\omega T_s}{2}\right) \Phi_{p1}^N(\omega).
\]

Because the power spectral density (PSD) of the differentiator, \( |\sin(\omega T_s/2)|^2 \), rejects the lower frequency components of \( \Phi_{p1}^N(\omega) \) the PSD of the \( \Delta\Phi_{p1}^N(t) \) contains almost no power assuming \( \Delta\nu \ll 1/T_s \).
A CW pump with an electric field of $P_2(t)$ is injected into the PPLN-2 waveguide to convert the SFG signal to the new signal $S_{out}(t)$:

$$S_{out}(t) \propto e^{i2\Phi_{P_1}(t)/|E_1|} e^{i\Delta \Phi_{D_{in}}(t)/|E_1|} + m e^{i3\Delta \Phi_{N_{in}}(t)/|E_1|},$$

where the value of $m$ is defined as $m = |E_2|/|E_1|$, and can be adjusted in the LCoS filter [7]. The term inside the brackets in Eq. (8) enables the function of squeezing the phase noise of the input signal.

Figure 2(a) shows the experimental setup for verifying the phase-noise-mitigation scheme. 20/30-Gbaud QPSK data is generated using a CW laser at 1550 nm. The signal is phase modulated with an ASE source to induce phase noise. The noisy signal is coupled with CW pump around 1551.5 nm and injected into PPLN-1 waveguide. A $\sim 450$-m HNLF-1 (ZDW at 1551.5 nm) is used to generate the third-order harmonics. A CW pump at 1543 nm is injected into the PPLN-2 waveguide to multiplex the signals. The generated signal is coupled with a CW pump around 1556.3 nm and injected into a 700-m dispersion stable HNLF-2 (ZDW at 1551.5 nm). The pump is phase modulated with 4.5-GHz data to suppress stimulated Brillouin scattering. Figure 2(c) shows the measured gain and output power profiles of HNLF-2.

The system performance is assessed using 20- and 30-Gbaud QPSK signals. Figure 3 shows the constellation diagrams of the 20-Gbaud input noisy signal and the output of the phase quantizer. The results are obtained for different values of phase noise. In order to compare the phase noise range between the constellation diagrams, the parameter $\delta \phi$ is defined to quantify the phase deviation from the corresponding expected value, showing the standard deviation of the phase. In addition, the parameter $\delta \rho$ is defined as the percentage of amplitude deviation from the expected value, showing the relative standard deviation of the amplitude. As can be seen in Fig. 3, phase noise is reduced by phase quantizer, in particular for higher levels of noise. In Fig. 3(a), $\delta \phi$ is reduced by $\sim 49\%$. The value of $\delta \rho$ is, however, increased by $\sim 56\%$. This indicates that phase noise is partially converted to amplitude noise in the phase quantizer. The amplitude noise can be suppressed by utilizing a parametric amplification in the saturation regime. Figure 4 shows the constellation diagrams of 30-Gbaud noisy QPSK signals, and the corresponding outputs of the phase quantizer, and the parametric amplifier. As can be seen, phase noise and amplitude noise are
decreased in the output of parametric amplifier. In Fig. 4(a), $\delta\phi$ is reduced by $\sim 40\%$ and $\delta\rho$ is reduced by $16\%$ in the output of parametric amplifier compared to the input signal. Figure 5(a) shows the percentage of phase-noise range reduction for various levels of phase noise for 30-Gbaud QPSK signal. The amount of reduction is increased for higher levels of phase noise, and it becomes gradually constant for the phase noise with $\delta\phi > 50^\circ$. Figure 5(b) shows the EVMs of the 30-Gbaud input noisy QPSK signal, and the corresponding outputs of the phase quantizer and the parametric amplifier for various levels of phase noise.

Figure 6 shows the BER curves of the phase noise mitigation scheme for two different levels of phase noise, $\delta\phi \sim 43^\circ$ and $\sim 55^\circ$. Near 1.5-dB OSNR gain is achieved in the phase quantizer output at BER of $10^{-3}$. By suppressing the amplitude noise in the parametric amplifier, near 3-dB OSNR gain is achieved at BER $10^{-3}$. An all-optical nonlinear phase noise mitigation is demonstrated based on the phase-locked multiplexing of signal harmonics and amplitude saturation, avoiding the need for phase-based feedback loops and injection locking. The phase-locking process converts the signal format to differential phase shift keying. Further studies are needed to investigate a phase-locked method without format conversion.

**Funding.** Center for Integrated Access Network (CIAN); National Science Foundation (NSF).

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